

Class Name : Math 127 - Fall 2020 - 3007

Instructor Name : Scheib

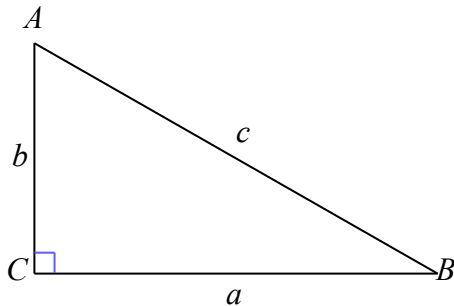
Student Name : Answer Key

Instructor Note :

**Question 1 of 16**

Solve the right triangle for the unknown sides and angles. Round values to 1 decimal place if necessary.

$$A = 28.3^\circ, a = 29$$



$$B = \underline{\hspace{2cm}}^\circ$$

$$b \approx \underline{\hspace{2cm}}$$

$$c \approx \underline{\hspace{2cm}}$$

**Question 2 of 16**

An aerial tram takes passengers from an elevation of 6314 ft to an elevation of 10,455 ft up the slope of a mountain. If the tram runs on a cable measuring 13,865 ft in length, what is the angle of incline of the tram to the nearest tenth of a degree?

The angle of incline of the tram is approximately                     °.

**Question 3 of 16**

Solve  $\triangle ABC$  subject to the given conditions, if possible. Round the lengths of the sides and measures of the angles (in degrees) to 1 decimal place if necessary. Round intermediate steps to at least four decimal places.

$$b = 88.5, c = 30, A = 108.5^\circ$$

- The triangle with these conditions does not exist.
- The triangle with these conditions does exist.

$a \approx$

\_\_\_\_\_

$B \approx$

\_\_\_\_\_

°

$C \approx$

\_\_\_\_\_

°

#### Question 4 of 16

Information is given about  $\triangle ABC$ . Determine if the information gives one triangle, two triangles, or no triangle. Solve the resulting triangle(s). Round the lengths of the sides and measures of the angles to 1 decimal place if necessary.

$$a = 48.1, c = 39.1, C = 24^\circ$$

- There is no triangle that can be formed from the given information.
- There is one unique triangle that can be formed from the given information.

$$A = \underline{\hspace{2cm}}^\circ$$

$$B \approx \underline{\hspace{2cm}}^\circ$$

$$b \approx \underline{\hspace{2cm}}$$

- There are two triangles that can be formed from the given information.

Triangle 1:

$$A \approx \underline{\hspace{2cm}}^\circ$$

$$B \approx \underline{\hspace{2cm}}^\circ$$

$$b \approx \underline{\hspace{2cm}}$$

Triangle 2:

$$A \approx \underline{\hspace{2cm}}^\circ$$

$$B \approx \underline{\hspace{2cm}}^\circ$$

$$b \approx \underline{\hspace{2cm}}$$

### Question 5 of 16

Plot the points whose polar coordinates are given.

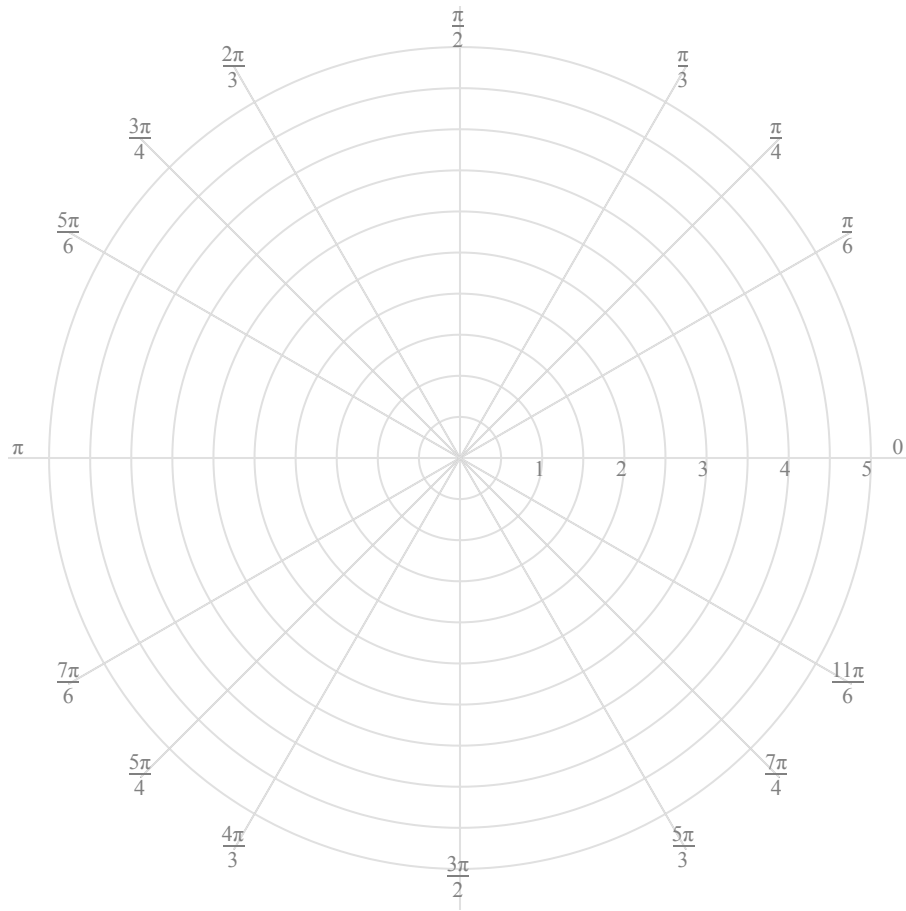
(a)  $\left(3, -\frac{5\pi}{6}\right)$

(b)  $(2, -\pi)$

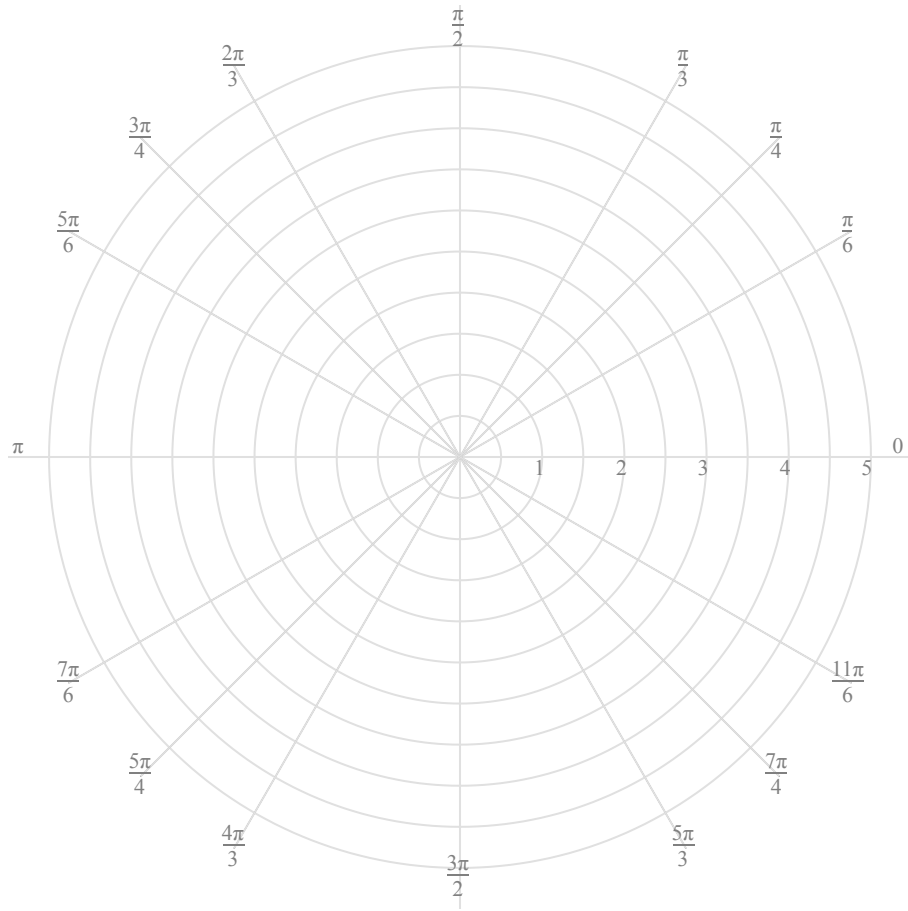
(c)  $\left(-4, -\frac{\pi}{3}\right)$

(d)  $\left(-5, -\frac{5\pi}{6}\right)$

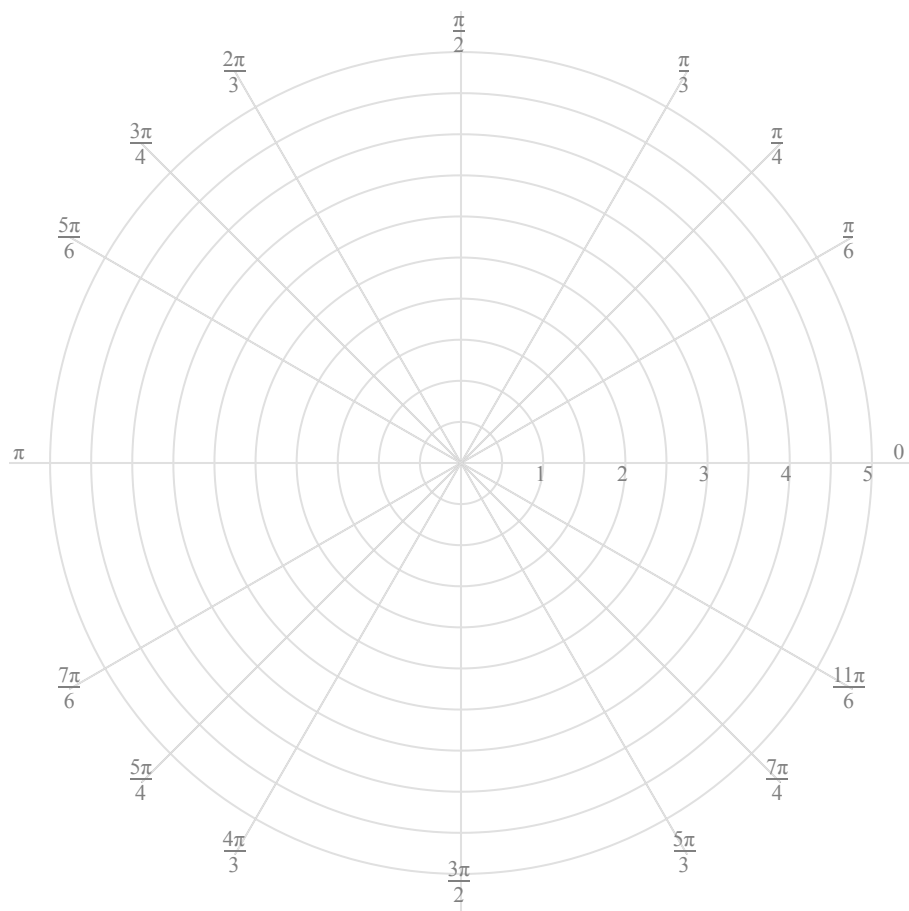
(a)  $\left(3, -\frac{5\pi}{6}\right)$



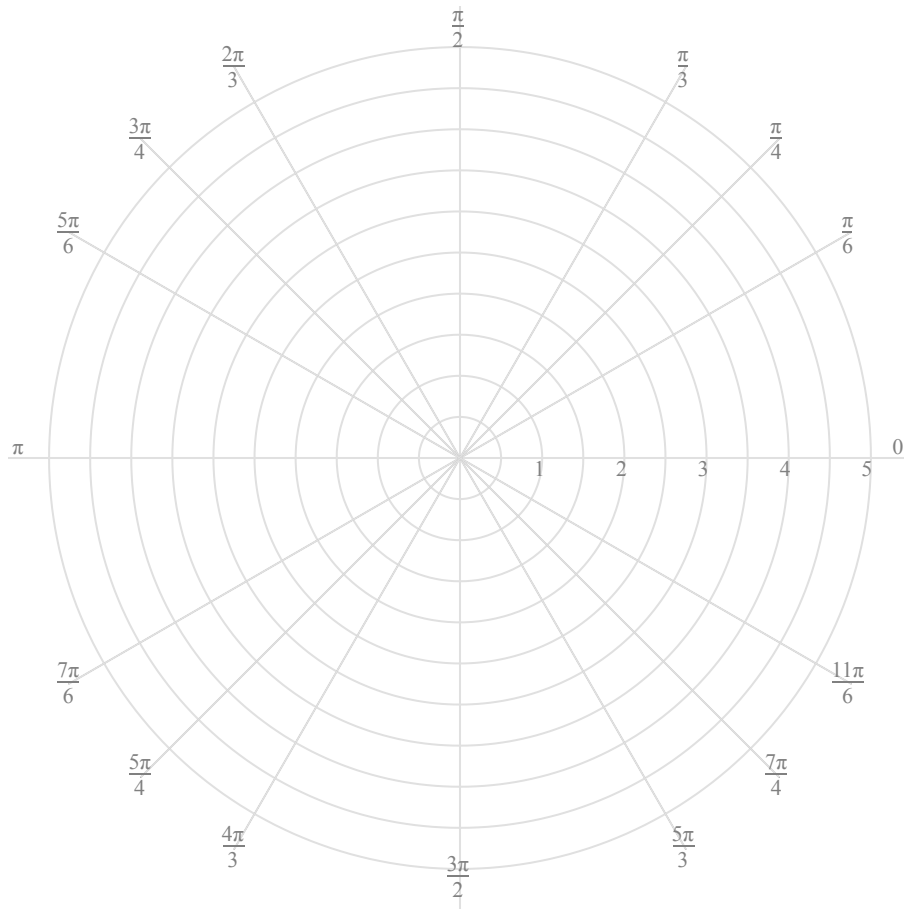
**(b)  $(2, -\pi)$**



(c)  $\left(-4, -\frac{\pi}{3}\right)$



(d)  $\left(-5, -\frac{5\pi}{6}\right)$



### Question 6 of 16

Given the point in polar coordinates  $\left(3.3, \frac{3\pi}{4}\right)$ , find two other polar coordinate representations.

#### Part 1 of 2

(a) Two other polar coordinate representations with  $r > 0$  and  $-2\pi \leq \theta \leq 3\pi$  are  
 $\left(\underline{\hspace{2cm}}, \underline{\hspace{2cm}}\right)$  and  $\left(\underline{\hspace{2cm}}, \underline{\hspace{2cm}}\right)$ .

(b) Two other polar coordinate representations with  $r < 0$  and  $-\pi \leq \theta \leq 2\pi$  are  
 ( \_\_\_\_\_ , \_\_\_\_\_ ) and ( \_\_\_\_\_ , \_\_\_\_\_ ).

### Question 7 of 16

Convert the ordered pair in polar coordinates to rectangular coordinates. Use exact values.  $\left(13, -\frac{\pi}{3}\right)$

The rectangular coordinates are (  ,  ).

### Question 8 of 16

Convert the ordered pair in rectangular coordinates to polar coordinates with  $r > 0$  and  $0 \leq \theta < 2\pi$ . Give the exact values for  $r$  and  $\theta$ .

$$(-7\sqrt{3}, 7)$$

Write your answer in simplest form.

The ordered pair in polar coordinates is ( \_\_\_\_\_ , \_\_\_\_\_ ).

### Question 9 of 16

Write an equivalent equation using polar coordinates.

$$x - 2y = 8$$

The polar equation is  $r =$  \_\_\_\_\_ .

### Question 10 of 16

Convert the polar equation to rectangular form and identify the type of curve represented.

$$r = 2 \sec \theta$$

Part 1 of 2

The type of curve represented is a \_\_\_\_\_ .  
(Blank 1)

Blank 1 Options

- horizontal line
- vertical line
- line that is nonhorizontal and nonvertical
- circle
- horizontal parabola
- vertical parabola

Part 2 of 2

Write the equation in standard form.

The rectangular form of the equation is .

**Question 11 of 16**

Vector  $\mathbf{v}$  has initial point  $P(1, 2)$  and terminal point  $Q(4, 11)$ . Vector  $\mathbf{w}$  has initial point  $R(-6, 1)$  and terminal point  $S(-3, 10)$ .

- Find the magnitude of  $\mathbf{v}$ . Give the exact answer.
- Find the magnitude of  $\mathbf{w}$ . Give the exact answer.
- Determine whether  $\mathbf{v} = \mathbf{w}$  and explain your reasoning.

Part 1 of 3

(a) Find the magnitude of  $\mathbf{v}$ . Give the exact answer.

$$\|\mathbf{v}\| = \underline{\hspace{2cm}}$$

Part 2 of 3

(b) Find the magnitude of  $\mathbf{w}$ . Give the exact answer.

$$\|\mathbf{w}\| = \underline{\hspace{2cm}}$$

Part 3 of 3

(c) Determine whether  $\mathbf{v} = \mathbf{w}$  and explain your reasoning.

$\mathbf{v}$                        $\mathbf{w}$ , since the vectors have                      magnitude and                      direction.  
(Blank 1) (Blank 2) (Blank 3)

Blank 1 Options

- =
- $\neq$

Blank 2 Options

- different
- the same

Blank 3 Options

- different
- the same

**Question 12 of 16**

Given a vector  $\mathbf{v}$  with initial point  $P(1, -3)$  and terminal point  $Q(3, -4)$ ,

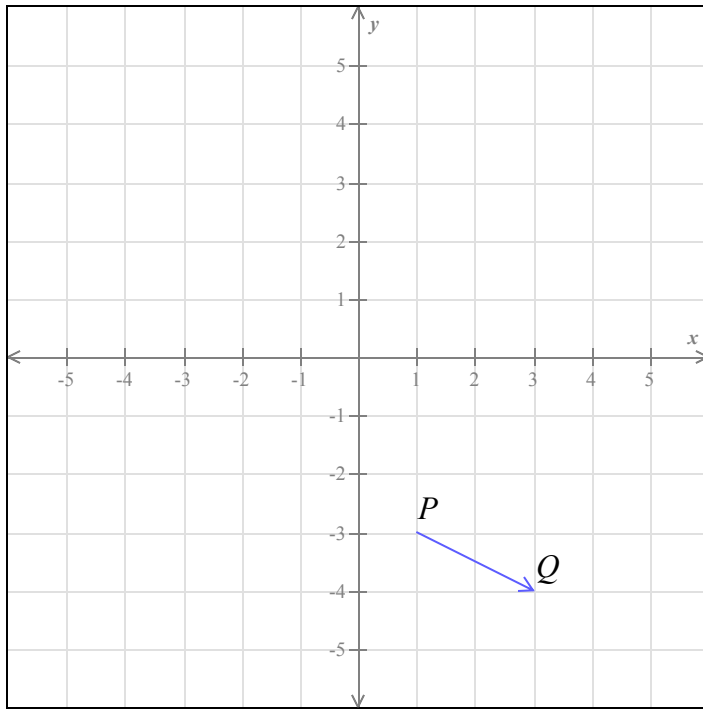
- (a) Write the component form of  $\mathbf{v}$ .
- (b) Sketch  $\mathbf{v}$  in standard position.

Part 1 of 2

(a) Write the component form of  $\mathbf{v}$ .

$$\langle \underline{\hspace{1cm}}, \underline{\hspace{1cm}} \rangle$$

(b) Sketch  $\mathbf{v}$  in standard position.



### Question 13 of 16

Given  $\mathbf{v} = \langle 8, -13 \rangle$  and  $\mathbf{r} = \langle 5, 9 \rangle$ ,

find  $\mathbf{v} - \mathbf{r}$ .

$$\mathbf{v} - \mathbf{r} = \langle \underline{\hspace{2cm}}, \underline{\hspace{2cm}} \rangle$$

### Question 14 of 16

Write the vector  $\mathbf{v}$  in the form  $a\mathbf{i} + b\mathbf{j}$ , where  $\mathbf{v}$  has the given magnitude and direction angle. Give your answer in exact form.

$$\|\mathbf{v}\| = \frac{3}{5}, \theta = 300^\circ$$

$$\mathbf{v} = \underline{\hspace{4cm}}$$

### Question 15 of 16

For  $\mathbf{r} = \mathbf{i} - 1.3\mathbf{j}$ , find the magnitude and direction angle for  $0^\circ \leq \theta \leq 360^\circ$ . Round to 1 decimal place.

$$\|\mathbf{r}\| \approx \underline{\hspace{2cm}}$$

$$\theta \approx \underline{\hspace{2cm}}^\circ$$

### Question 16 of 16

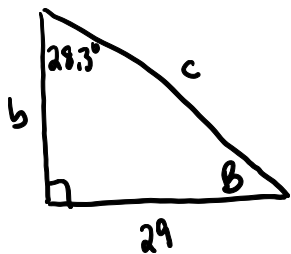
Determine if the vectors  $\mathbf{p} = \langle 6, 18 \rangle$  and  $\mathbf{q} = \langle -3, -9 \rangle$  are orthogonal, parallel, or neither.

$\mathbf{p}$  and  $\mathbf{q}$  are                     .  
(Blank 1)

Blank 1 Options

- orthogonal
- parallel
- neither

1)

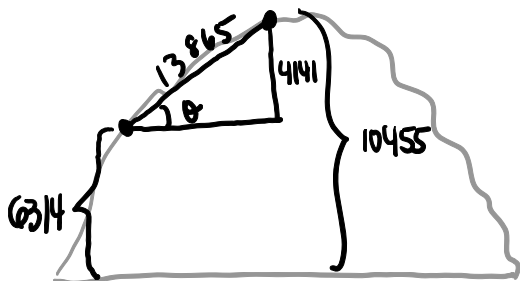


$$\tan 28.3^\circ = \frac{29}{b} \Rightarrow b = \frac{29}{\tan 28.3^\circ} = 53.9$$

$$\sin 28.3^\circ = \frac{29}{c} \Rightarrow c = \frac{29}{\sin 28.3^\circ} = 61.2$$

$$28.3^\circ + B + 90^\circ = 180^\circ \Rightarrow B = 61.7^\circ$$

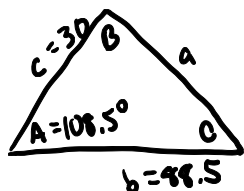
2)



$$10455 - 6314 = 4141$$

$$\sin \theta = \frac{4141}{13865} \Rightarrow \theta = \sin^{-1}\left(\frac{4141}{13865}\right) = 17.4^\circ$$

3)

SAS  $\Rightarrow$  Law of Cosines

$$a^2 = 88.5^2 + 30^2 - 2(88.5)(30)\cos 108.5^\circ = 10417.1377$$

$$a = \sqrt{10417.1377} = 102.1$$

$$30^2 = 102.1^2 + 88.5^2 - 2(102.1)(88.5)\cos C$$

$$900 = 18256.66 - 18071.7 \cos C$$

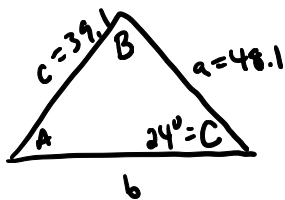
$$-17356.66 = -18071.7 \cos C$$

$$\cos C = 0.9604$$

$$C = \cos^{-1}(0.9604) = 16.2^\circ$$

$$108.5^\circ + B + 16.2^\circ = 180^\circ \Rightarrow B = 55.3^\circ$$

4)

SSA  $\Rightarrow$  Law of Sines

$$\frac{\sin 24^\circ}{39.1} \neq \frac{\sin A}{48.1}$$

$$39.1 \sin A = 48.1 \sin 24^\circ$$

$$\sin A = \frac{48.1 \sin 24^\circ}{39.1} = 0.5004$$

$$A = \sin^{-1}(0.5004) = 30.3^\circ$$

$$30.3^\circ + B + 24^\circ = 180^\circ \Rightarrow B = 125.7^\circ$$

$$\frac{\sin 24^\circ}{39.1} \times \frac{\sin 125.7^\circ}{b}$$

$$b \sin 24^\circ = 39.1 \sin 125.7^\circ$$

$$b = \frac{39.1 \sin 125.7^\circ}{\sin 24^\circ} = 78.1$$

$$A_2 = 180^\circ - 30.3^\circ = 149.7^\circ$$

$$149.7^\circ + B_2 + 24^\circ = 180^\circ \Rightarrow B_2 = 6.3^\circ$$

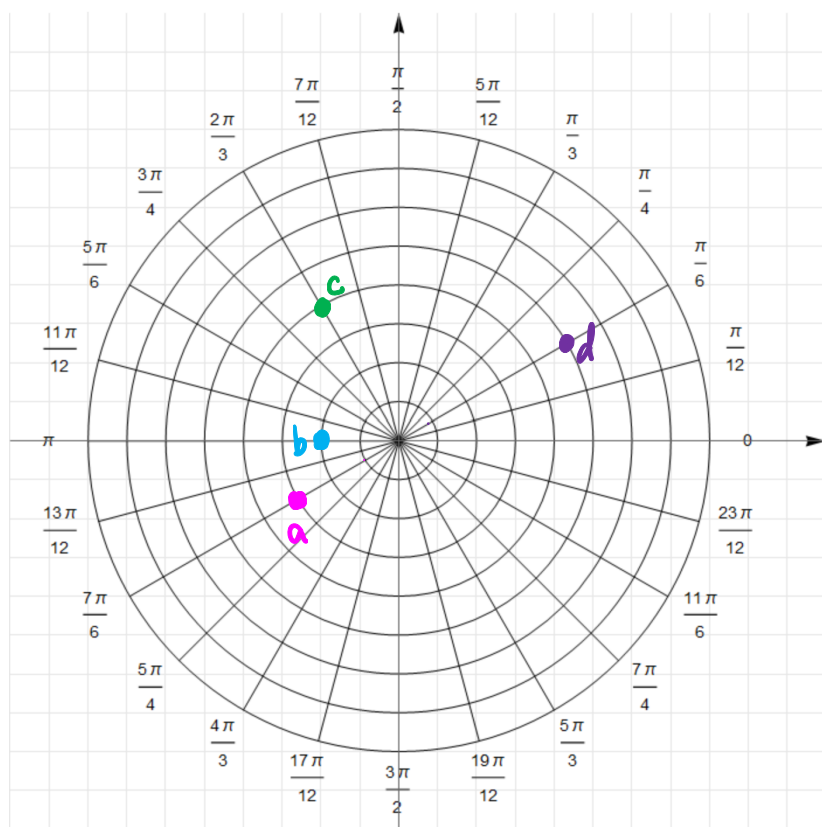
2<sup>nd</sup> triangle exists

$$\frac{\sin 24^\circ}{39.1} \times \frac{\sin 6.3^\circ}{b}$$

$$b \sin 24^\circ = 39.1 \sin 6.3^\circ$$

$$b = \frac{39.1 \sin 6.3^\circ}{\sin 24^\circ} = 10.5$$

5)



$$6) a) \frac{3\pi}{4} + 2\pi = \frac{3\pi}{4} + \frac{8\pi}{4} = \frac{11\pi}{4}$$

$$(3.3, \frac{11\pi}{4})$$

$$\frac{3\pi}{4} - 2\pi = \frac{3\pi}{4} - \frac{8\pi}{4} = -\frac{5\pi}{4}$$

$$(3.3, -\frac{5\pi}{4})$$

$$b) \frac{3\pi}{4} + \pi = \frac{3\pi}{4} + \frac{4\pi}{4} = \frac{7\pi}{4}$$

$$(-3.3, \frac{7\pi}{4})$$

$$\frac{3\pi}{4} - \pi = \frac{3\pi}{4} - \frac{4\pi}{4} = -\frac{\pi}{4}$$

$$(-3.3, -\frac{\pi}{4})$$

$$7) x = r \cos \theta = 13 \cos(-\frac{\pi}{3}) = 13 \left(\frac{1}{2}\right) = \frac{13}{2}$$

$$y = r \sin \theta = 13 \sin(-\frac{\pi}{3}) = 13 \left(-\frac{\sqrt{3}}{2}\right) = -\frac{13\sqrt{3}}{2}$$

$$\left(\frac{13}{2}, -\frac{13\sqrt{3}}{2}\right)$$

$$8) r = \sqrt{x^2 + y^2} = \sqrt{(-7\sqrt{3})^2 + 7^2} = \sqrt{147 + 49} = \sqrt{196} = 14$$

$$\theta = \tan^{-1}\left(\frac{y}{x}\right) = \tan^{-1}\left(\frac{7}{-7\sqrt{3}}\right) = \tan^{-1}\left(-\frac{\sqrt{3}}{3}\right) = -\frac{\pi}{6}$$

$$(-7\sqrt{3}, 7) = \text{quadrant II} \Rightarrow \theta = -\frac{\pi}{6} + \pi = \frac{5\pi}{6}$$

$$(14, \frac{5\pi}{6})$$

$$9) \underbrace{x}_{r \cos \theta} - 2 \underbrace{y}_{r \sin \theta} = 8$$

$$r \cos \theta - 2r \sin \theta = 8$$

$$r(\cos \theta - 2 \sin \theta) = 8$$

$$r = \frac{8}{\cos \theta - 2 \sin \theta}$$

$$10) r = 2 \sec \theta$$

$$r = \frac{2}{\cos \theta}$$

$$\frac{r \cos \theta}{x} = 2$$

$x = 2 \Rightarrow$  vertical line

$$11) \vec{v} = \langle 4-1, 11-2 \rangle = \langle 3, 9 \rangle$$

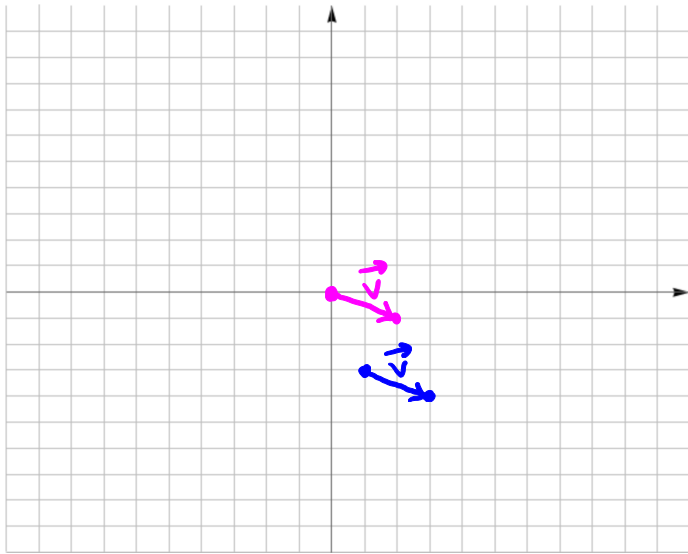
$$\vec{w} = \langle -3-(-6), 10-1 \rangle = \langle 3, 9 \rangle$$

$$a) \|\vec{v}\| = \sqrt{3^2 + 9^2} = \sqrt{9+81} = \sqrt{90} = 3\sqrt{10}$$

$$b) \|\vec{w}\| = 3\sqrt{10}$$

c)  $\vec{v} = \vec{w}$ , since the vectors have the same magnitude and same direction

$$12) \vec{v} = \langle 3-1, -4-(-3) \rangle = \langle 2, -1 \rangle$$



$$13) \vec{v} - \vec{r} = \langle 8-5, -13-9 \rangle = \langle 3, -22 \rangle$$

$$14) x = \|\vec{v}\| \cos \theta = \frac{3}{5} \cos 300^\circ = \frac{3}{5} \left(\frac{1}{2}\right) = \frac{3}{10}$$

$$y = \|\vec{v}\| \sin \theta = \frac{3}{5} \sin 300^\circ = \frac{3}{5} \left(-\frac{\sqrt{3}}{2}\right) = -\frac{3\sqrt{3}}{10}$$

$$\vec{v} = \frac{3}{10} \vec{i} - \frac{3\sqrt{3}}{10} \vec{j}$$

$$15) \|\vec{r}\| = \sqrt{1^2 + (-1.3)^2} = \sqrt{1 + 1.69} = \sqrt{2.69} = 1.6$$

$$\theta = \tan^{-1}\left(\frac{-1.3}{1}\right) = \tan^{-1}(-1.3) = -52.4^\circ$$

$$\vec{r} = \langle 1, -1.3 \rangle \Rightarrow \text{quad IV} \Rightarrow \theta = -52.4^\circ \text{ or } -52.4^\circ + 360^\circ = 307.6^\circ$$

$$16) \vec{p} \cdot \vec{q} = \langle 6, 18 \rangle \cdot \langle -3, -9 \rangle = 6(-3) + 18(-9) = -180$$

$$\vec{p} \cdot \vec{p} = \langle 6, 18 \rangle \cdot \langle 6, 18 \rangle = 6(6) + 18(18) = 360$$

$$\|\vec{p}\| = \sqrt{360} = 6\sqrt{10}$$

$$\vec{q} \cdot \vec{q} = \langle -3, -9 \rangle \cdot \langle -3, -9 \rangle = (-3)(-3) + (-9)(-9) = 90$$

$$\|\vec{q}\| = \sqrt{90} = 3\sqrt{10}$$

$$\cos \theta = \frac{-180}{6\sqrt{10} \cdot 3\sqrt{10}} = \frac{-180}{180} = -1$$

$$\theta = \cos^{-1}(-1) = 180^\circ \Rightarrow \text{parallel}$$